# Ontology Integration Using Mappings: Towards Getting the Right Logical Consequences (Technical Report, December 12, 2008) 

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#### Abstract

We propose a general method and novel algorithmic techniques to facilitate the integration of independently developed ontologies using mappings. Our method and techniques aim at helping users understand and evaluate the semantic consequences of the integration, as well as to detect and fix potential errors. We also present ContentMap, a system that implements our approach, and a preliminary evaluation which suggests that our approach is both useful and feasible in practice.


## 1 Introduction

Effective ontology integration techniques are often needed both during ontology development (e.g., when an ontology being developed reuses a set of external ontologies), and when ontologies are used in conjunction with data (e.g. when integrating and querying data sources annotated using different ontologies).

When the ontologies to be integrated have been independently developed, their vocabularies are most likely going to diverge, either because they use different namespaces, or because they use different names or naming conventions for referring to their entities. As a consequence, these ontologies will most likely be unrelated from a logical point of view, even if they intuitively overlap.

For example, suppose that Peter wants to develop an ontology about juvenile forms of arthritis ${ }^{3}$. He finds on the Web two independently developed ontologies $\mathcal{O}_{1}$ and $\mathcal{O}_{2}$ with different vocabularies, which describe different types of arthritis and juvenile diseases respectively, and decides that an integration of these two ontologies would make a good starting point. Although largely independent, the two ontologies do overlap; for example, both describe a particular form of juvenile arthritis known as JRA (Juvenile Rheumatoid Arthritis), although they use different vocabulary in their descriptions.

As a first step in the integration of such independently developed ontologies it is usually necessary to establish appropriate correspondences (or mappings) between the terms used in the various ontologies. For example, Peter may need

[^0]to establish that Rheumatoid_Arthritis in $\mathcal{O}_{1}$ has the same intended meaning as Rheum_Arthritis in $\mathcal{O}_{2}$. Ontologies are, however, often too large and complex for ontology developers to manually establish these correspondences. To address this problem, a number of sophisticated tools have been developed (see http: //www.ontologymatching.org/ for a comprehensive list), the purpose of which is to (semi-) automatically establish appropriate correspondences.

When reasoning with the ontologies to be integrated together with the automatically generated mappings, however, errors are likely to occur. There are two main causes for these errors. On the one hand, mappings suggested by automated tools are likely to include some errors. On the other hand, even if the correct mappings have been found, the ontologies may contain conflicting descriptions of the overlapping entities. These errors manifest themselves as unintended logical consequences (e.g., unsatisfiable concepts or unintended subsumptions), and they can be difficult to detect, understand and repair. However, existing tools provide little or no support for the user in trying to obtain the right logical consequences when integrating ontologies using mappings. Indeed, as discussed in Section 5 , research in this area is still at an early stage $[1,2]$.

In this paper, we present a new general method and novel algorithmic techniques to facilitate the integration of independently developed ontologies using mappings. We also present ContentMap, ${ }^{4}$ a system that implements our approach, and a preliminary evaluation which suggests that our approach is both useful and feasible in practice. We assume some basic knowledge of OWL and Description Logics, and refer to [3, 4] for comprehensive overviews.

## 2 Problems with Ontology Integration using Mappings

In this section, we discuss some of the problems that arise when integrating ontologies using mappings, and analyze the requirements for suitable tools.

Let us consider the ontologies $\mathcal{O}_{1}$ and $\mathcal{O}_{2}$ from Section 1 about arthritis and juvenile diseases respectively. As already mentioned, $\mathcal{O}_{1}$ and $\mathcal{O}_{2}$ overlap in the description of different types of juvenile rheumatoid arthritis. The overlapping parts of $\mathcal{O}_{1}$ and $\mathcal{O}_{2}$ are shown in Table 1.

Suppose that Peter-the ontology developer-uses an automatic mapping tool to find correspondences between entities in $\mathcal{O}_{1}$ and $\mathcal{O}_{2}$. Mappings are often represented as a tuple $\left\langle i d, e_{1}, e_{2}, n, \rho\right\rangle$ [5], where $i d$ is a unique identifier for the mapping, $e_{1}, e_{2}$ are entity names in the vocabulary of $\mathcal{O}_{1}$ and $\mathcal{O}_{2}$ respectively, $n$ a numeric confidence measure between 0 and 1 , and $\rho$ a relation between $e_{1}$ and $e_{2}$ (typically subsumption ( $Б$ ), equivalence $(\equiv)$, or disjointness $(\perp)$ ).

Table 2 contains the mappings obtained by Peter using the mapping tool OLA (see http://ola.gforge.inria.fr/). The prefixes ' 1 :' and ' 2 :' for the entity names refer to the namespaces (omitted in Table 1) of $\mathcal{O}_{1}$ and $\mathcal{O}_{2}$. Note that the mappings and confidence values suggested by different tools can vary enormously, so experience and/or experimentation may be needed in order to select the most suitable tool (or combination of tools) for the problem at hand.

[^1]Table 1. Example Ontologies

| Ontology $\mathcal{O}_{1}$ |  |
| :---: | :---: |
|  | Juvenile_Arthritis $\sqsubseteq$ Systemic_Disease $\square$ Rheumatoid_Arthritis |
| $\alpha_{2}$ | Multi_Joint_Disease $\sqsubseteq$ Disease $\Pi \geqslant 5$ affects.Joint |
| $\alpha_{3}$ | Rheumatoid_Arthritis $\sqsubseteq$ Disease $\square \exists$ has_Factor. $\top$ |
| $\alpha_{4}$ | Poly_Juvenile_Arthritis $\sqsubseteq$ Juvenile_Arthritis $\square$ Multi_Joint_Disease |
| $\alpha_{5}$ | Oly_Juvenile_Arthritis $\sqsubseteq$ Juvenile_Arthritis $\square \neg$ Poly_Juvenile_Arthritis |
|  | Oly_Juvenile_Arthritis $\sqsubseteq \forall$ has_Factor.Negative_Factor |
| $\alpha_{7}$ | Negative_Factor $\Pi$ Positive_Factor $\sqsubseteq \perp$ |
| Ontology $\mathcal{O}_{2}$ |  |
| $\beta_{1}$ | Juv_Rheum_Arthritis $\sqsubseteq$ Rheum_Arthritis $\square$ Juv_Disease |
| $\beta_{2}$ | Rheum_Arthritis $\sqsubseteq$ Disease $\square \exists$ has_Rheum_Factor. $\rceil$ |
| $\beta_{3}$ | Poly_Juv_Rheum_Arthritis $\sqsubseteq$ Juv_Rheum_Arthritis $\Pi=3$ affects. Joint |
| $\beta_{4}$ | Poly_Juv_Rheum_Arthritis $\sqsubseteq \forall h a s \_$Rheum_Factor.Positive_Rheum_Factor |
| $\beta_{5}$ | Negative_Rheum_Factor $\square$ Positive_Rheum_Factor $\sqsubseteq \perp$ |

Table 2. Example Mappings

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Intended Mappings
\(\left\langle\mu_{1}, 1\right.\) :Joint, 2:Joint, 1.0, ( \(\equiv\) ) \(\rangle\);
\(\left\langle\mu_{2}, 1\right.\) :Disease, 2:Disease, 1, ( \(\equiv\) ) \(\rangle\);
\(\left\langle\mu_{3}, 1\right.\) :Disease, 2:Disease, 1.0, (三) \(\rangle\);
\(\left\langle\mu_{4}, 1\right.\) :affects, 2:affects, 0.87, ( \(\equiv\) ) \(\rangle\);
\(\left\langle\mu_{5}, 1:\right.\) Rheumatoid_Arthritis, 2:Rheum_Arthritis, 1.0, \(\left.(\equiv)\right\rangle\);
\(\left\langle\mu_{6}, 2\right.\) :Juv_Disease, 1:Disease, 0.63 , ( \(\left.\left.\sqsubseteq\right)\right\rangle\);
\(\left\langle\mu_{7}, 1\right.\) :Poly_Juvenive_Arthritis, 2:Poly_Juv_Rheum_Arthritis, 0.7 , ( \(\equiv\) ) \(\rangle\);
\(\left\langle\mu_{8}, 1\right.\) :has_Factor, 2:has_Rheum_Factor, \(\left.0.7,(\equiv)\right\rangle\);
\(\left\langle\mu_{9}, 1\right.\) :Positive_Factor, 2:Positive_Rheum_Factor, \(\left.0.75,(\equiv)\right\rangle\);
\(\left\langle\mu_{10}, 1\right.\) :Negative_Factor, 2:Negative_Rheum_Factor, \(\left.0.75,(\equiv)\right\rangle\);
\(\left\langle\mu_{11}\right.\), 2:Juv_Rheum_Arthritis, 1:Rheumatoid_Arthritis, 0.5, ( \(\sqsubseteq\) ) \(\rangle\);
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Erroneous Mappings
$\left\langle\mu_{12}, 1:\right.$ Rheumatoid_Arthritis, 2:Juv_Rheum_Arthritis, 0.5 , ( ()$\rangle$;
$\left\langle\mu_{13}, 1\right.$ :Disease, 2:Juv_Disease, 0.63 , (Б) $\rangle$;
$\left\langle\mu_{14}, 1\right.$ :Positive_Factor, 2:Negative_Rheum_Factor, $\left.0.63,(\equiv)\right\rangle$;
$\left\langle\mu_{15}, 2\right.$ :Positive_Factor, 1:Negative_Rheum_Factor, $\left.0.63,(\equiv)\right\rangle$;

As shown in Table 2, some of the mappings are clearly erroneous and, under any reasonable semantics for the mappings, will lead to unintended logical consequences. Indeed, the mappings $\mu_{14}$ and $\mu_{15}$ entail the logical equivalence of two concepts that are disjoint in both $\mathcal{O}_{1}$ and $\mathcal{O}_{2}$ (see also intended mappings $\mu_{9}$ and $\mu_{10}$ ); also, the mapping $\mu_{12}$ will lead to unintended subsumptions since not all forms of rheumatoid arthritis affect only children. Furthermore, even if only
intended mappings had been generated, errors would still have occurred due to conflicting descriptions of some of the entities that occur in both ontologies. For example, the descriptions of Polyarticular Juvenile Rheumatoid Arthritis (axioms $\alpha_{4}, \alpha_{2}$ in $\mathcal{O}_{1}$ and $\beta_{3}$ in $\mathcal{O}_{2}$ ) are contradictory: in $\mathcal{O}_{1}$ it is described as a disease that affects at least 5 different joints, whereas in $\mathcal{O}_{2}$ it is said to affect exactly 3 joints. The intended mapping $\mu_{7}$ will reveal this contradiction.

This example suggests some requirements for a tool supporting ontology integration using mappings. A suitable tool should provide support for: (i) generating sets of mappings, either manually or by selecting one or more mapping algorithms and setting their parameters; (ii) editing sets of mappings and filtering them according to different criteria; (iii) reasoning with the ontologies to be integrated together with the relevant mappings; (iv) comparing the entailments holding before and after the integration and detecting possible unintended entailments; $(v)$ suggesting possible ways to repair the identified errors.

## 3 Proposed Method, Algorithms and Tool Support

In this paper, we present a novel approach for integrating ontologies using mappings that addresses the requirements from Section 2. To this end, a formal representation of ontology mappings should be adopted. This is crucial, for example, to reason unambiguously with the mappings together with the ontologies to be integrated, and thus to address requirements (iii)-(v) in Section 2.

A number of specialised semantics for ontology mappings have been proposed in the literature (e.g. [5, 6]). In this paper, however, we have chosen to represent ontology mappings as OWL 2 axioms [4]. Such a representation seems semantically coherent, and allows us to reuse the extensive range of OWL algorithmic techniques and infrastructure that is currently available. The general approach we present here, however, could be adapted to alternative formal representations of mappings (see Section 5 for further discussion).

We assume from now on that a set of mappings is represented as an OWL 2 ontology, where mappings $\left\langle i d, e_{1}, e_{2}, n, \rho\right\rangle$ are given as axioms of the form SubClassOf $\left(e_{1} e_{2}\right)$, EquivalentClasses $\left(e_{1} e_{2}\right)$, or DisjointClasses $\left(e_{1} e_{2}\right)$, for $\rho$ of the form $(\sqsubseteq)$, $(\equiv)$, or $(\perp)$ respectively, with $i d$ (the mapping id) and $n$ (the confidence value) added as axiom annotations [4]. We denote with $\operatorname{conf}(\alpha)$ the confidence value with which an axiom $\alpha$ is annotated. Representing mappings in this way gives them a standard "crisp" semantics, with ids and confidence values being represented only as annotations and thus having no effect on entailments.

Our general approach is given at a high level in Figure 1 and formally in Table 3. It is an interactive process where some steps involve computations that tools should perform automatically, while others (marked with $(\star)$ ) may require manual intervention. It consists of four main parts: i) Computation of mappings (Steps 1-3); ii) Computation of new entailments (Steps 4-6); iii) Detection of errors (Step 7); iv) Repair of the identified errors (Steps 8-12). We next present our method and describe its realisation in ContentMap-a Protégé 4 plugin available for download (see [7]).

Table 3. Ontology Integration Method
Input: $\mathcal{O}_{1}, \mathcal{O}_{2}$ : ontologies with $\operatorname{Sig}\left(\mathcal{O}_{1}\right)=\Sigma_{1}, \operatorname{Sig}\left(\mathcal{O}_{2}\right)=\Sigma_{2}$ and $\Sigma_{1} \cap \Sigma_{2}=\emptyset$
Output: $\mathcal{O}_{1}^{\prime}, \mathcal{O}_{2}^{\prime}$ : modified ontologies
$\mathcal{M}^{\prime}$ : Mappings between $\Sigma_{1}$ and $\Sigma_{2}$
1: ( $\star$ ) Select mapping algorithm $\operatorname{map}\left(\mathcal{O}_{1}, \mathcal{O}_{2}\right)$
2: $(\star)$ Select $\mathcal{M} \subseteq \operatorname{map}\left(\mathcal{O}_{1}, \mathcal{O}_{2}\right)$
3: $(\star)$ if $\mathcal{O}_{1}, \mathcal{O}_{2}, \mathcal{M}$ satisfactory, then return $\mathcal{O}_{1}^{\prime}:=\mathcal{O}_{1}, \mathcal{O}_{2}^{\prime}:=\mathcal{O}_{2}, \mathcal{M}^{\prime}:=\mathcal{M}$
4: $\mathcal{U}:=\mathcal{O}_{1} \cup \mathcal{O}_{2} \cup \mathcal{M}$
5: ( $\star$ ) Select approximation functions diff $\approx$ and mdiff $\approx$
6: Compute $\Lambda=\operatorname{diff} \widetilde{\Sigma}_{1}\left(\mathcal{O}_{1}, \mathcal{U}\right) \cup \operatorname{diff} \widetilde{\Sigma}_{2}\left(\mathcal{O}_{2}, \mathcal{U}\right) \cup \operatorname{mdiff} \widetilde{\Sigma}_{1}, \Sigma_{2}(\mathcal{M}, \mathcal{U})$
7: $(\star)$ Select $\Im^{+}, \Im^{-} \subseteq \Lambda$
8: ( $\star$ ) Select $\mathcal{O}^{-} \subseteq \mathcal{U}$
9: $\mathbb{P}:=$ all minimal plans for $\mathcal{U}$ given $\Im^{+}, \Im^{-}$, and $\mathcal{O}^{-}$
10: $(\star)$ if no satisfactory plan in $\mathbb{P}$, then come back to either Step 2 or Step 7
11: ( $\star$ ) Select $\mathcal{P} \in \mathbb{P}$
12: return $\mathcal{O}_{1}^{\prime}:=\mathcal{O}_{1} \backslash \mathcal{P}, \mathcal{O}_{2}^{\prime}:=\mathcal{O}_{2} \backslash \mathcal{P}, \mathcal{M}^{\prime}:=\mathcal{M} \backslash \mathcal{P}$


Fig. 1. Merging Method (Informal). Numbers Refer to Table 3

### 3.1 Computation of the Mappings

General Description Ontology mappings can be computed using one or more mapping tools (see Step 1), and can subsequently be refined (Step 2) in various ways (e.g., via manual selection or filtering according to a given threshold). After obtaining and possibly refining the mappings, a user may decide that the integration process is complete (Step 3), in which case it remains a purely syntactic process. They may, however, want to analyse the semantic consequences of the integration, in which case a reasoner is required.

Tool Support ContentMap provides for the input ontologies to be loaded, and for one or more mapping tools to be selected. Different weights can also be assigned to each of the mapping tools. It is also possible to load pre-computed mappings in the form of an OWL 2 ontology.


Fig. 2. GUI for Visualising Explicit Mappings in ContentMap

ContentMap provides a GUI for visualising the mappings (Fig. 2) and showing those that are to be accepted (marked with $\checkmark$ ) and those that are to be rejected (marked with $\otimes$ ). Users can automatically filter the mappings by setting a confidence threshold $\tau$ : mappings with a confidence value lower than $\tau$ are automatically marked for rejection while those with a confidence value greater than $\tau$ are marked for acceptance. These selections can then be refined at will.

### 3.2 Computation of New Entailments

General Description To help users understand the semantic consequences of the integration, they should be informed about new entailments that hold in the merged ontology $\mathcal{U}$, but not in $\mathcal{O}_{1}, \mathcal{O}_{2}$ and $\mathcal{M}$ alone. To this end, we use the notion of deductive difference $[8,9]$. Intuitively, the deductive difference between $\mathcal{O}$ and $\mathcal{O}^{\prime}$ w.r.t a signature $\Sigma$ is the set of entailments constructed over $\Sigma$ that do not hold in $\mathcal{O}$, but do hold in $\mathcal{O}^{\prime}$.

Example 1. Assume that $\mathcal{O}_{1}$ and $\mathcal{O}_{2}$ are as in Table 1 and $\mathcal{M}_{S}$ contains the mappings in Table 2. Let $\mathcal{U}=\mathcal{O}_{1} \cup \mathcal{O}_{2} \cup \mathcal{M}_{S}$. There are entailments expressed using the vocabulary of $\mathcal{O}_{1}$ (respectively $\mathcal{O}_{2}$ ) only, which hold in $\mathcal{U}$ and not in $\mathcal{O}_{1}$ (respectively $\mathcal{O}_{2}$ ); for example, $\sigma_{1}:=$ (respectively $\sigma_{2}:=$ ). Furthermore, there are mappings that hold in $\mathcal{U}$, but not in $\mathcal{M}_{S}$ alone (e.g. $\sigma_{3}:=$ ).

Definition 2. Let $\mathcal{D} \mathcal{L}$ be a $D L$ and $\Sigma$ be a $\mathcal{D} \mathcal{L}$-signature. The $\Sigma$-deductive difference between $\mathcal{D} \mathcal{L}$-ontologies $\mathcal{O}$ and $\mathcal{O}^{\prime}$ is given as follows:

$$
\begin{equation*}
\operatorname{diff}_{\Sigma}\left(\mathcal{O}, \mathcal{O}^{\prime}\right)=\left\{\alpha \mid \alpha \text { a } \mathcal{D} \mathcal{L} \text {-axiom, } \mathcal{O} \not \vDash \alpha, \mathcal{O}^{\prime} \vDash \alpha \text { and } \operatorname{Sig}(\alpha) \subseteq \Sigma\right\} \tag{1}
\end{equation*}
$$

In our integration scenario, we want to inform the user about new entailments that hold in $\mathcal{O}_{1}$ or $\mathcal{O}_{2}$ as a result of the integration, i.e., $\operatorname{diff}_{\Sigma_{1}}\left(\mathcal{O}_{1}, \mathcal{U}\right)$ and $\operatorname{diff}_{\Sigma_{2}}\left(\mathcal{O}_{2}, \mathcal{U}\right)$. In our example from Tables 1 and 2 , where the mappings are given as an OWL 2 ontology as described above, the entailments (Positive_Factor $\sqsubseteq \perp$ ) and (Rheum_Arthritis $\sqsubseteq$ Juv_Disease) belong to $\operatorname{diff}_{\Sigma_{1}}\left(\mathcal{O}_{1}, \mathcal{U}\right)$ and diff $\Sigma_{\Sigma_{2}}\left(\mathcal{O}_{2}, \mathcal{U}\right)$ respectively. In addition, we want to inform the user about new entailments that contain symbols from both $\mathcal{O}_{1}$ and $\mathcal{O}_{2}$. These entailments can be seen as inferred mappings provided that the notion of a mapping is generalised to be an arbitrary DL axiom using terms from two signatures:

Definition 3. Let $\mathcal{D} \mathcal{L}$ be a $D L$ and let $\Sigma_{1}, \Sigma_{2}$ be two $\mathcal{D} \mathcal{L}$-signatures s.t. $\Sigma_{1} \cap$ $\Sigma_{2}=\{\top, \perp\}$. Let $\Sigma=\Sigma_{1} \cup \Sigma_{2}$. A $\mathcal{D} \mathcal{L}$-mapping between $\Sigma_{1}, \Sigma_{2}$ is a $\mathcal{D} \mathcal{L}$-axiom $\alpha$ over $\Sigma$ such that $\left(\operatorname{Sig}(\alpha) \cap \Sigma_{i}\right) \backslash\{\top, \perp\} \neq \emptyset$ for each $i \in\{1,2\}$. The axiom $\alpha$ is annotated with an id and with a confidence value $0<\operatorname{conf}(\alpha) \leq 1$. Definition 2 can now be extended to take into account the new mappings.

$$
\begin{equation*}
\operatorname{mdiff}_{\Sigma_{1}, \Sigma_{2}}\left(\mathcal{O}, \mathcal{O}^{\prime}\right)=\left\{\alpha \in \operatorname{diff}_{\Sigma}\left(\mathcal{O}, \mathcal{O}^{\prime}\right) \mid \alpha \mathcal{D} \mathcal{L} \text {-mapping between } \Sigma_{1}, \Sigma_{2}\right\} \tag{2}
\end{equation*}
$$

In our scenario, inferred mappings are captured by $\operatorname{mdiff}_{\Sigma_{1}, \Sigma_{2}}(\mathcal{M}, \mathcal{U})$. For example, the mapping (1:Juvenile_Arthritis $\sqsubseteq 2:$ Rheum_Arthritis) would belong to this difference, because it is entailed by $\mathcal{U}$ but not by $\mathcal{M}$ alone.

The notion of deductive difference, however, has several drawbacks in practice. First, there is no algorithm for computing $\operatorname{diff}\left(\mathcal{O}, \mathcal{O}^{\prime}\right)$ in expressive DLs, such as $\mathcal{S R O I Q}$ (OWL 2) and $\mathcal{S H O \mathcal { O }}$ (OWL DL) [9]. For these languages, checking whether $\operatorname{diff}\left(\mathcal{O}, \mathcal{O}^{\prime}\right)=\emptyset$ is undecidable. Currently, algorithms only exist for (fragments of) the OWL 2 EL and QL profiles [10, 9, 8]. Second, the number of entailments in the difference can be huge (even infinite), and so likely to overwhelm users. These drawbacks motivate the need for approximationssubsets of the difference - that the user can select in Step 5 from Table 3.

Definition 4. A function $\operatorname{diff} \approx \tilde{\tilde{\Sigma}}\left(\mathcal{O}, \mathcal{O}^{\prime}\right)$ (resp. mdiff $\tilde{\Sigma}_{1}, \Sigma_{2}\left(\mathcal{O}, \mathcal{O}^{\prime}\right)$ ) is an approximation for $\operatorname{diff}_{\Sigma}\left(\mathcal{O}, \mathcal{O}^{\prime}\right)\left(\right.$ mdiff $\left._{\Sigma_{1}, \Sigma_{2}}\left(\mathcal{O}, \mathcal{O}^{\prime}\right)\right)$ if for each $\mathcal{D} \mathcal{L}$-ontologies $\mathcal{O}, \mathcal{O}^{\prime}$, $\operatorname{diff} \approx \tilde{\Sigma}\left(\mathcal{O}, \mathcal{O}^{\prime}\right) \subseteq \operatorname{diff}_{\Sigma}\left(\mathcal{O}, \mathcal{O}^{\prime}\right)\left(\operatorname{mdiff}_{\Sigma_{1}, \Sigma_{2}}\left(\mathcal{O}, \mathcal{O}^{\prime}\right) \subseteq \operatorname{mdiff}_{\Sigma_{1}, \Sigma_{2}}\left(\mathcal{O}, \mathcal{O}^{\prime}\right)\right)$.

Tool Support A useful approximation should be easy to compute, yet still provide meaningful information to the user. One possibility is to define an approximation by considering only entailments of a certain form.

The GUI implemented in ContentMap allows users to customise approximations by selecting among the following simple kinds of entailments, where $A, B$ are atomic concepts (including $\top, \perp$ ) and $R, S$ atomic roles or inverses of atomic roles: (i) $A \sqsubseteq B$, (ii) $A \sqsubseteq \neg B$, (iii) $A \sqsubseteq \exists R . B$, (iv) $A \sqsubseteq \forall R . B$, and v) $R \sqsubseteq S$. The smallest implemented approximation considers only axioms of the form (i), while the largest one considers all types (i)— (v).

All these approximations can be algorithmically computed, and ContentMap uses a number of optimisations for computing them. Clearly, the larger the class of entailments presented to the user, the more errors could be detected. The corresponding differences, however, are harder to compute, harder to present to the user, and may be harder for the user to understand.

### 3.3 Detection of Errors

General Description Some entailments in the relevant (approximate) differences may be intended, while others may reveal potential errors in the merged ontology $\mathcal{U}$. Step 7 therefore involves selecting entailments that: (i) are intended and should be entailed in $\mathcal{U}$ (written $\Im^{+}$in Table 3), and (ii) are unintended and should not be entailed by $\mathcal{U}$ (written $\Im^{-}$).

In our example, the entailments (Positive_Factor $\sqsubseteq \perp$ ) and (Rheum_Arthritis $\sqsubseteq$ Juv_Disease) in $\operatorname{diff}_{\Sigma_{1}}\left(\mathcal{O}_{1}, \mathcal{U}\right)$ and $\operatorname{diff}_{\Sigma_{2}}\left(\mathcal{O}_{2}, \mathcal{U}\right)$ respectively are unintented and should belong to $\Im^{-}$. In contrast, the entailed mapping (1:Rheum_Arthritis $\sqsubseteq$ 2:Disease) is intended and should be included in $\Im^{+}$.

Tool Support The development of techniques to help users understand the relevant differences and subsequently select the sets of intended and unintended entailments is especially challenging.

First, the tool should explain why the new entailments that hold in $\mathcal{U}$ do not hold in $\mathcal{O}_{1}, \mathcal{O}_{2}$ and $\mathcal{M}$ alone. The notion of a justification has proved very useful in understanding why an ontology entails a certain axiom [11, 12].

Definition 5. Let $\mathcal{O} \models \alpha$. A justification for $\alpha$ in $\mathcal{O}$ is an ontology $\mathcal{O}^{\prime} \subseteq \mathcal{O}$ satisfying the following properties: (i) $\mathcal{O}^{\prime} \models \alpha$, and (ii) there is no $\mathcal{O}^{\prime \prime} \subset \mathcal{O}^{\prime}$ s.t. $\mathcal{O}^{\prime \prime} \vDash \alpha$. We denote by $\operatorname{Just}(\alpha, \mathcal{O})$ the set of all justifications for $\alpha$ in $\mathcal{O}$.

In order to explain a given entailment, ContentMap presents all its justifications. Computing justifications is expensive, so ContentMap uses the optimisations proposed in $[13,14]$ which have proved effective in practice.

Second, the potentially large number of relevant entailments may overwhelm the user. Hence, on the one hand, these entailments should be presented in a friendly way and, on the other hand, the tool should provide suggestions about which entailments to include in $\Im^{+}$and $\Im^{-}$.

ContentMap exploits the dependencies between entailments to organise the way in which they are displayed. Intuitively an entailment $\beta$ depends on $\alpha$ in $\mathcal{O}$ if, whenever $\alpha$ is invalidated by removing a set of axioms from $\mathcal{O}$, then $\beta$ is also invalidated. This implies that if $\alpha \in \Im^{-}$, then $\beta$ should also be included in $\Im^{-}$ (and never in $\Im^{+}$). This idea can be formalised in our setting as follows:

Definition 6. Let $\mathcal{O} \models \alpha, \beta$. The axiom $\beta$ depends on $\alpha$ w.r.t. $\mathcal{O}$, written $\alpha \triangleright \beta$ iff for each $\mathcal{J}_{\beta} \in \operatorname{Just}(\beta, \mathcal{O})$, there is $\mathcal{J}_{\alpha} \in \operatorname{Just}(\alpha, \mathcal{O})$ s.t. $\mathcal{J}_{\alpha} \subseteq \mathcal{J}_{\beta}$.

The relation $\triangleright$ is consistent with our intuitions, as shown next:
Proposition 7. Consider Table 3 and Definition 6. Let $\mathcal{U} \vDash \alpha, \beta, \mathcal{U}^{\prime} \subset \mathcal{U}$ and $\alpha \triangleright \beta$. Then: 1) $\mathcal{U}^{\prime} \not \vDash \alpha$ implies $\mathcal{U}^{\prime} \not \models \beta$, and 2) $\mathcal{U}^{\prime} \models \beta$ implies $\mathcal{U}^{\prime} \models \alpha$.

Proof. First we prove Condition 1. Let $\alpha \triangleright \beta$ and $\mathcal{U}^{\prime} \not \vDash \alpha$. Since $\mathcal{U} \models \alpha$, for each $\mathcal{J}_{\alpha} \in \operatorname{Just}(\alpha, \mathcal{U})$ there is an axiom $\gamma \in \mathcal{J}_{\alpha}$ s.t. $\gamma \notin \mathcal{U}^{\prime}$. Otherwise, $\mathcal{U}^{\prime}$ would imply $\alpha$. Let $\mathcal{J}_{\beta} \in \operatorname{Just}(\beta, \mathcal{U})$. By definition of $\triangleright$, there must be a $\mathcal{J}_{\alpha} \in \operatorname{Just}(\alpha, \mathcal{U})$ s.t. $\mathcal{J}_{\alpha} \subseteq \mathcal{J}_{\beta}$. Since $\mathcal{U}^{\prime}$ does not include one axiom from each $\mathcal{J}_{\alpha}$, then it also does not include one axiom from each $\mathcal{J}_{\beta}$ and therefore $\mathcal{U}^{\prime} \not \vDash \beta$, as required.

We now prove Condition 2. Let $\alpha \triangleright \beta$ and $\mathcal{U}^{\prime} \models \beta$. Since $\mathcal{U} \vDash \beta$, there is a $\mathcal{J}_{\beta} \in \operatorname{Just}(\beta, \mathcal{U})$ s.t. $\mathcal{J}_{\beta} \subseteq \mathcal{U}^{\prime}$. By definition of $\triangleright$ there must exist a $\mathcal{J}_{\alpha} \in$ $\operatorname{Just}(\alpha, \mathcal{U})$ s.t. $\mathcal{J}_{\alpha} \subseteq \mathcal{J}_{\beta}$. Therefore $\mathcal{J}_{\alpha} \in \mathcal{U}^{\prime}$ and $\mathcal{U}^{\prime} \models \alpha$, as required.

```
Algorithm 1 Heuristic suggestions for \(\Im^{+}, \Im^{-}\)
Input: \(\Lambda=\operatorname{diff} \widetilde{\Sigma}_{1}\left(\mathcal{O}_{1}, \mathcal{U}\right) \cup \operatorname{diff} \widetilde{\Sigma}_{2}\left(\mathcal{O}_{2}, \mathcal{U}\right) \cup \operatorname{mdiff} \widetilde{\Sigma}_{1}, \Sigma_{2}(\mathcal{M}, \mathcal{U})\) as in Table 3
\(\tau_{1}, \tau_{2}\) : real values with \(0<\tau_{1} \leq \tau_{2} \leq 1\)
\(\triangleright\) : dependency relation between axioms in \(\Lambda\) w.r.t. \(\mathcal{U}\)
Output: \(\Im^{+}, \Im^{-}\): entailments suggested to be hold or not
    \(\Im^{+}, \Im^{-}:=\emptyset\)
    for each \(\alpha \in \Lambda\) do
        if \(\alpha\) of the form \(A \sqsubseteq \perp\) for \(A\) an atomic concept then
            \(\Im^{-}:=\Im^{-} \cup\{\alpha\}\)
            for each \(\beta \in \Lambda\) such that \(\alpha \triangleright^{*} \beta\) do \(\Im^{-}:=\Im^{-} \cup\{\beta\}\)
        end if
        \(\operatorname{conf}(\alpha):=\) confidence of \(\alpha\) as in Definition 8
        if \(\operatorname{conf}(\alpha) \leq \tau_{1}\) then \(\Im^{-}:=\Im^{-} \cup\{\alpha\}\)
        if \(\operatorname{conf}(\alpha) \geq \tau_{2}\) and \(\alpha \notin \Im^{-}\)then \(\Im^{+}:=\Im^{+} \cup\{\alpha\}\)
    end for
    return \(\Im^{+}, \Im^{-}\)
```

In order to suggest to users which entailments to include in $\Im^{+}$and $\Im^{-}$, ContentMap exploits both the dependencies between entailments in the differences and the confidence values for each explicit mapping. We use the confidence values in the mappings to compute confidence values in the entailments from each of the obtained differences. We consider our confidence in an entailment to be equal to the maximum confidence we have in one of its justifications, and our confidence in a justification to be the product of our confidences in each of the axioms it contains. We formalise this in the following definition, in which we extend $\operatorname{conf}()$ to arbitrary (explicit) axioms and justifications: by defining $\operatorname{conf}(\alpha)=1$ in case $\alpha$ is not a mapping, i.e., if $\alpha$ is not annotated with a confidence value:

Definition 8 (Confidence in an Entailment). Let $\mathcal{O}$ be an ontology, $\alpha$ an axiom in $\mathcal{O}$ that is not annotated with a confidence value, $\mathcal{J}$ a justification, and $\beta$ an entailment s.t. $\mathcal{O} \models \beta$. We define $\operatorname{conf}(\alpha)=1$, and $\operatorname{conf}(\mathcal{J})$ and $\operatorname{conf}(\beta)$ as follows:

$$
\begin{equation*}
\operatorname{conf}(\mathcal{J})=\prod_{\gamma \in \mathcal{J}} \operatorname{conf}(\gamma) \quad \text { and } \quad \operatorname{conf}(\beta)=\max \left(\bigcup_{\mathcal{J} \in \operatorname{Just}(\beta, \mathcal{O})} \operatorname{conf}(\mathcal{J})\right) \tag{3}
\end{equation*}
$$

The following proposition shows that the confidence values in Definition 8 are well-behaved w.r.t. Definition 6: if $\beta$ depends on $\alpha$ then the confidence on $\beta$ is smaller than the confidence on $\alpha$.

Proposition 9. If $\alpha \triangleright^{*} \beta$, then $\operatorname{conf}(\beta) \leq \operatorname{conf}(\alpha)$
Proof. if $\alpha \triangleright^{*} \beta$, then for each $\mathcal{J}_{\beta} \in \operatorname{Just}(\beta, \mathcal{U})$ there must exist a $\mathcal{J}_{\alpha} \in \operatorname{Just}(\alpha, \mathcal{U})$ s.t. $\mathcal{J}_{\alpha} \subseteq \mathcal{J}_{\beta}$. By definition of $\operatorname{conf}(\mathcal{J})$ (see Definition 8), it is immediate to see that $\operatorname{conf}\left(\mathcal{J}_{\beta}\right) \leq \operatorname{conf}\left(\mathcal{J}_{\alpha}\right)$. Thus, for each $\mathcal{J}_{\beta} \in \operatorname{Just}(\beta, \mathcal{U})$ there must exist a $\mathcal{J}_{\alpha} \in \operatorname{Just}(\alpha, \mathcal{U})$ s.t. $\operatorname{conf}\left(\mathcal{J}_{\beta}\right) \leq \operatorname{conf}\left(\mathcal{J}_{\alpha}\right)$. By Definition 8 it is immediate to see that $\operatorname{conf}(\beta) \leq \operatorname{conf}(\alpha)$.

| new entailents wrt signature of ontology 1 |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Negative Factor |  |  |  |  |  |
| - Negative_Factor subClassof Nothing (c: 0.4688 ) |  |  |  |  |  |
| Positive_Fator |  |  |  |  |  |
| - Positive_Factor subclass Of Nothing (c:0.4688) |  |  |  |  |  |
| Oly_Juverile_Athitis |  |  |  |  |  |
| Oly_Juvenile_Arthritis subClassof Nothing (c:0.4688) |  |  |  |  |  |
| New Mapping entalents (01 $\rightarrow$ O2) |  |  |  |  |  |
| Juvenile_Athtritis |  |  |  |  |  |
| OJA1:Juvenile_Arthritis subClassof JIA2:Rheum_Arthritis (c: 0.8125 ) (1)0 |  |  |  |  |  |
| - JIA1:Juvenile_Arthritis subClassof JIAz:Juv_Rheum_Arthritis (c: 0.5 ; © |  |  |  |  |  |
| Multi_Joit_ Dise |  |  |  |  |  |
| - JIA1:Multi_Joint_Disease subClassof JIAZ:Juv_Disease (c: 0.625) |  |  |  |  |  |
| - JIA1:Multi_Joint_Disease subclassof JIA2:Disease (c: 1.0) |  |  |  |  |  |
| Rheumatoid_Arthitis |  |  |  |  |  |
| -JIA1:Rheumatoid_Arthritis subClassof JIA2:Juv_Disease (c:0.625) |  |  |  |  |  |
| - JIA1:Rheumatoid_Arthritis subClassof JIA2:Disease (c: 1.0) |  |  |  |  |  |


| new entallents wrt signature of ontology 2 |  |  |
| :---: | :---: | :---: |
| Negative_Rheum_Factor |  |  |
| - Negative_Rheum_Factor subClassof Nothing | (c: 0.4688$)$ | 0 |
| Postive_Rheum_Fator |  |  |
| - Positive_Rheum_Factor subclassof Nothing | (c: 0.4688 ) | ©0 |
| Rheum_Athitis |  |  |
| -Rheum_Arthritis subclassof Juv_Disease (c: | (c: 0.625) | $\boldsymbol{*}$ |
| Poly_Juv_Reum_Atrritis |  |  |
| - Poly_Juv_Rheum_Arthritis subClassof Nothing | g (c:0.4688) | 0 |
| NEW MAPPING ENTALENTS ( $02 \rightarrow 01$ ) |  |  |
| Rheum_Athitis |  |  |
| - JIAZ:Rheum_Arthritis subClassof JIA1:Disease | (c: 1.0) | (1)0 |
| Juv_Rheum_Athritis |  |  |
| - JIA2:Juv_Rheum_Arthritis subClassof JIA1:Disea | sease (c: 1.0) | 3 |
| Sstemic_Juv_Rheum_Athritis |  |  |
| JIA2:Systemic_Juv_Rheum_Arthritis subClassOf JIA1:Rheumatoid_Arthritib ©0.8125 ) |  |  |

Fig. 3. GUI for Visualising New Entailments in ContentMap

(a) Dependency Relation

(b) Justifications

Fig. 4. GUI for Visualising the Dependency Relation and the Justifications

In order to compute initial suggestions for $\Im^{-}$and $\Im^{+}$, ContentMap implements the heuristics in Algorithm 1, which are based on Definitions 6, 8 and Propositions 7, 9. The algorithm accepts as input the entailments in the relevant differences, their dependencies, and two confidence thresholds $\tau_{1}$ and $\tau_{2}$. For each input entailment $\alpha$, Algorithm 1 uses $\triangleright, \tau_{1}$ and $\tau_{2}$ to either include it in $\Im^{+}$(i.e. $\alpha$ is intended), in $\Im^{-}$(i.e. $\alpha$ is unintended) or in neither of them. An entailment $\alpha$ is included in $\Im^{-}$if it either reveals a contradiction (Line 3), or it depends on a contradiction (Line 5), or its confidence according to Definition 8 is lower than $\tau_{1}$ (Line 8). In contrast, $\alpha$ is included in $\Im^{+}$if it is not contained in $\Im^{-}$and its confidence is higher than the threshold $\tau_{2}$ (Line 9).

Figures 3 and 4 show the ContentMap GUI for selecting $\Im^{+}$and $\Im^{-}$. Figure 3 shows the new entailments in each of the computed differences. The left-hand side of Figure 4(a) displays the dependency relation as a hierarchy, which can be expanded and contracted in the usual way; on the right-hand side of Figure 4(a), the user can select an entailment to be in $\Im^{+}$or $\Im^{-}$and show its justifications
(Figure 4(b)). When displaying justifications, the GUI indicates whether the axioms in these justifications come from $\mathcal{O}_{1}, \mathcal{O}_{2}$, or the mappings $\mathcal{M}$ (marked with ' 1 ', ' 2 ' and ' M ' respectively). The entailments in Figures 3 and 4(a) already marked as intended/unintended are those suggested by Algorithm 1.

### 3.4 Repair

General Description If the user has selected one or more unintended entailments (i.e., $\Im^{-} \neq \emptyset$ ), then $\mathcal{U}$ clearly contains errors. These errors can always be repaired by removing axioms from $\mathcal{U}$-in the limit, removing all the axioms from $\mathcal{U}$ will eliminate all entailments. However, any removal of axioms should also respect $\Im^{+}$, the user's selection of intended entailments, i.e., the entailments in $\Im^{+}$should still hold after any removal of axioms.

As mentioned in Section 1, errors could be due to erroneous mappings, to inherently conflicting information in the two ontologies, or to some combination of both. Repairing such errors might, therefore, require the removal of axioms from $\mathcal{M}, \mathcal{O}_{1}$ and $\mathcal{O}_{2}$. The user may, however, have a (principled or pragmatic) preference regarding the source of axioms to be removed; e.g., $\mathcal{M}$ might be considered the most likely source of errors, or it may be impossible to change (one or both of) $\mathcal{O}_{1}$ and $\mathcal{O}_{2}$. We therefore define the notion of a repair plan (or plan for short) for an ontology $\mathcal{O}$ w.r.t. the (un-) intended entailments $\Im^{-}$and $\Im^{+}$, and a subset $\mathcal{O}^{-}$of $\mathcal{O}$, where the axioms in $\mathcal{O}^{-}$are those that are allowed to be removed from $\mathcal{O}$. Such a plan is simply a subset of the axioms in $\mathcal{O}^{-}$whose removal from $\mathcal{O}$ both eliminates the entailments in $\Im^{-}$and preserves those in $\Im^{+}$. In general, there may be zero or more such plans.

Definition 10. Let $\mathcal{O}, \Im^{+}, \Im^{-}$, and $\mathcal{O}^{-}$be finite sets of axioms such that $\mathcal{O}^{-} \subseteq$ $\mathcal{O}, \mathcal{O} \models \Im^{-}, \mathcal{O} \models \Im^{+}$, and $\Im^{+} \cap \Im^{-}=\emptyset$.

A repair plan for $\mathcal{O}$ given $\mathcal{O}^{-}, \Im^{+}$and $\Im^{-}$is a set $\mathcal{P} \subseteq \mathcal{O}^{-}$such that: 1) $(\mathcal{O} \backslash \mathcal{P}) \vDash \alpha$ for each $\alpha \in \Im^{+}$, and 2) $(\mathcal{O} \backslash \mathcal{P}) \not \models \beta$ for each $\beta \in \Im^{-}$. A plan $\mathcal{P}$ is minimal if there is no $\mathcal{P}_{1}$ such that $\mathcal{P}_{1} \subset \mathcal{P}$.

In our method, $\Im^{-}, \Im^{+}$and $\mathcal{O}^{-}$are selected by the user in Steps 7 and 8 from Table 3. In our example, if Peter imports $\mathcal{O}_{1}$ and $\mathcal{O}_{2}$ from the Web, and if he is not willing to copy and modify them (e.g., if he wants to always import the latest versions), then plans should only remove axioms from the mappings (i.e., $\mathcal{O}^{-}=\mathcal{M}$ ). However, the descriptions of Polyarticular Juvenile Rheumatoid Arthritis in $\mathcal{O}_{1}$ and $\mathcal{O}_{2}$ are inherently in contradiction and hence, if $\mathcal{O}^{-}=\mathcal{M}$, the corresponding error cannot be fixed without deleting reasonable mappings. In this case a more sensible choice would be to repair one or both of $\mathcal{O}_{1}$ and $\mathcal{O}_{2}$.

Tool Support Definition 10 suggests a simple procedure for computing all plans: for each possible $\mathcal{P} \subseteq \mathcal{O}^{-}$, use a reasoner to check if $\mathcal{P}$ is a valid plan, i.e., satisfies Conditions 1 and 2 from Definition 10. ContentMap, however, implements an algorithm (see Algorithm 2) that avoids potentially expensive entailment checks by reusing the justifications already computed when obtaining the

```
Algorithm 2 Computing All Plans Using Justifications
Procedure all_Plans \(\left(\mathcal{O}, \mathcal{O}^{-}, \Im^{+}, \Im^{-}\right)\)
Input: \(\mathcal{O}, \mathcal{O}^{-}, \Im^{+}, \Im^{-}\)as in Definition 10, Just \((\gamma, \mathcal{O})\) for each \(\gamma \in \Im^{+} \cup \Im^{-}\)
Output: P: set of all plans
    \(\mathbf{P}:=\emptyset\)
    for each \(\mathcal{P} \subseteq \mathcal{O}^{-}\)do
        validPlan \(:=\) true
        for each \(\alpha \in \Im^{+}\)do
            foundJust := false
            for each \(\mathcal{J}_{\alpha} \in \operatorname{Just}(\alpha, \mathcal{O})\) do
                if \(\mathcal{J}_{\alpha} \subseteq \mathcal{O} \backslash \mathcal{P}\) then foundJust \(:=\) true
            end for
            if foundJust \(=\) false then validPlan \(:=\) false
        end for
        for each \(\beta \in \Im^{-}\)and \(\mathcal{J}_{\beta} \in \operatorname{Just}(\beta, \mathcal{O})\) do
            if \(\mathcal{J}_{\beta} \subseteq \mathcal{O} \backslash \mathcal{P}\) then validPlan := false
        end for
        if validPlan \(=\) true then \(\mathbf{P}:=\mathbf{P} \cup\{\mathcal{P}\}\)
    end for
    return \(P\)
```

dependency relation from Definition 6. The algorithm is based on the following principles: (i) in order for $\alpha \in \Im^{+}$to hold after the execution of a plan, $\mathcal{P}$, the ontology $\mathcal{O} \backslash \mathcal{P}$ must contain at least one justification for $\alpha$ in $\mathcal{O}$ (see Lines (6-8)); (ii) in order for $\beta \in \Im^{-}$not to hold after the execution of $\mathcal{P}$, it is sufficient to show that no justification for $\beta$ in $\mathcal{O}$ is in $\mathcal{O} \backslash \mathcal{P}$ (Lines 11-13). The set of all minimal plans can be straightforwardly computed once all the plans have been obtained.

Proposition 11. Algorithm 2 computes all the plans for $\mathcal{O}$ given $\mathcal{O}^{-}, \Im^{+}, \Im^{-}$.
Proof. For any $\mathcal{P} \in \mathbf{P}$ we show that $\mathcal{P}$ is a plan for $\mathcal{O}$ given $\mathcal{O}^{-}, \Im^{+}$and $\Im^{-}$, as per Definition 10. The facts that $\mathcal{P} \subseteq \mathcal{O}^{-}$is clear from Line 2. For each $\alpha \in \Im^{+}$, Line 7 implies that there is a justification $\mathcal{J}_{\alpha} \in \operatorname{Just}(\alpha, \mathcal{O})$ s.t. $\mathcal{J}_{\alpha} \in \mathcal{O} \backslash \mathcal{P}$, and the definition of justification immediately implies that $\mathcal{P}$ satisfies Condition 1 from Definition 10. For each $\beta \in \Im^{-}$, Lines 14 and 15 imply that $\mathcal{P}$ removes at least one axiom from each justification for $\beta$ in $\mathcal{O}$, which implies that $\mathcal{P}$ also satisfies Condition 2.

Let us assume that there exists a plan $\mathcal{P}$ for $\mathcal{O}$ given $\mathcal{O}^{-}, \Im^{+}$and $\Im^{-}$. This means that either there is an $\alpha \in \Im^{+}$s.t. no justification for $\alpha$ in $\mathcal{O}$ is contained in $\mathcal{O} \backslash \mathcal{P}$, or there is a $\beta \in \Im^{-}$and a justification $\mathcal{J}_{\beta}$ for $\beta$ in $\mathcal{O}$ s.t. $\mathcal{J}_{\beta} \subseteq \mathcal{O} \backslash \mathcal{P}$. In the first case, there can be no justification for $\alpha$ in $\mathcal{O} \backslash \mathcal{P}$, because $\mathcal{O} \backslash \mathcal{P} \subseteq \mathcal{O}$, so $\mathcal{O} \backslash \mathcal{P} \not \vDash \alpha$, contradicting our assumption that $\mathcal{P}$ is a plan. In the second case, $\mathcal{J}_{\beta} \in \mathcal{O} \backslash \mathcal{P}$, which implies $\mathcal{O} \backslash \mathcal{P} \models \beta$, also contradicting our assumption.

Note that conflicting choices in $\Im^{+}$and $\Im^{-}$may make it impossible to find any plans. Some of these conflicts can be detected using the dependency relation $\triangleright$, as shown in the following proposition:


Fig. 5. Selection of Plans

Proposition 12. Let $\mathcal{O}, \Im^{+}, \Im^{-}$and $\mathcal{O}^{-}$be as in Definition 10 and let $\mathcal{O} \vDash$ $\alpha$, $\beta$. If $\alpha \triangleright^{*} \beta$ w.r.t. $\mathcal{O}, \alpha \in \Im^{-}$and $\beta \in \Im^{+}$, then no plan exists.

Proof. Assume that $\alpha \in \Im^{-}, \beta \in \Im^{+}$, and that there is a plan $\mathcal{P}$ for $\mathcal{O}$ given $\mathcal{O}^{-}, \Im^{+}$and $\Im^{-}$. From the definition of a plan, $\mathcal{O}^{\prime}=\mathcal{O} \backslash \mathcal{P}$ is s.t. $\mathcal{O}^{\prime} \neq \alpha$, and from Proposition $7, \mathcal{O} \not \models \beta$. However, since $\beta \in \Im^{+}$, we also have that $\mathcal{O}^{\prime} \models \beta$, contradicting our assumption that $\mathcal{P}$ is a plan.

There may also be particular selections of $\mathcal{O}^{-}, \Im^{+}$and $\Im^{-}$for which the number of minimal plans is very large. In this case, selecting the most suitable minimal plan becomes difficult for users.

In order to assist users in the selection of a minimal plan (Steps 10-11), ContentMap implements a number of heuristics based on the confidence of the mappings in the plans and the total number of axioms in the plan, among others. The GUI in ContentMap for displaying and selecting minimal plans is shown in Figure 5. The axioms are marked according to their provenance (in the figure, they are all mappings and hence are marked with ' M '). Axioms that occur in all minimal plans are additionally marked with a ' P '. ContentMap ranks the plans in order of confidence, extending the definition of confidence to a plan $\mathcal{P}$ as follows: $\operatorname{conf}(\mathcal{P})=\prod_{\alpha \in \mathcal{P}} \operatorname{conf}(\alpha)$.Obviously, minimal plans with low rank are preferred for execution because they involve deleting mappings with lowest confidence.

## 4 Evaluation

In our experiments, we used a suite of four ontologies adapted from the 2004 EON Ontology Alignment Contest ${ }^{5}$ which describe the domain of bibliographic references. These ontologies have been developed independently by INRIA ( $\mathcal{O}_{\text {INR }}$ ), MIT ( $\mathcal{O}_{\text {MIT }}$ ), UMBC ( $\mathcal{O}_{\mathrm{UMBC}}$ ) and AIFB Karlsruhe ( $\mathcal{O}_{\text {AIFB }}$ ) respectively. Their sizes vary from 58 classes, 46 object properties, 26 data properties and 235 axioms in $\mathcal{O}_{\text {AIFB }}$ to 18 classes, 12 object properties, 19 data properties and 96

[^2]axioms in $\mathcal{O}_{\mathrm{UMBC}}$. Even if small, all these ontologies are fairly expressive $\left(\mathcal{O}_{\text {INR }}\right.$ and $\mathcal{O}_{\text {MIT }}$ are expressible in the $\mathrm{DL} \mathcal{A L C H} \mathcal{Q}(\mathcal{D}), \mathcal{O}_{\mathrm{UMBC}}$ in $\mathcal{A L C I N}(\mathcal{D})$ and $\mathcal{O}_{\text {AIFB }}$ in $\mathcal{A L C I}(\mathcal{D})$ respectively). Their average classification time is less than a second when using Pellet 1.5.

In the 2004 EON contest, $\mathcal{O}_{\text {INR }}$ was used as reference ontology, and the other ontologies were independently aligned with it using each of the competing tools. For evaluation, a manually produced gold standard containing the agreed-upon, correct mappings was provided for each pair of aligned ontologies. The gold standards for $\mathcal{O}_{\text {MIT }}, \mathcal{O}_{\text {UMBC }}$ and $\mathcal{O}_{\text {AIFB }}$ contain 119,83 and 98 mappings respectively. All the test ontologies and gold standards are available at our web page [7].

The experiments are organised in two parts, which we specify next, and were performed on a laptop with a 1.82 GHz processor and 3 GB of RAM.

Repair of Ontologies Using Gold Standard First, we have evaluated the semantic consequences of integrating each of $\mathcal{O}_{\text {MIT }}, \mathcal{O}_{\text {UMBC }}$ and $\mathcal{O}_{\text {AIFB }}$ with $\mathcal{O}_{\text {INR }}$ using the corresponding gold standard to detect inherent disagreements between them. In each case we have applied our method from Table 3, with the mappings in Step 2 being the corresponding gold standard. We have used both the smallest and the largest approximations of the deductive differences implemented in ContentMap (see Section 3.2), and obtained the following results.

1. Alignment $\mathcal{O}_{\mathrm{MIT}}, \mathcal{O}_{\mathrm{INR}}$ : for the smallest (resp. the largest) approximation, there were 3 (resp. 33) new entailments in $\mathcal{O}_{\text {MIT }}, 13$ (resp. 85) in $\mathcal{O}_{\text {INR }}$ and 35 (resp. 189) new mappings.
2. Alignment $\mathcal{O}_{\mathrm{UMBC}}, \mathcal{O}_{\text {INR }}$ : for the smallest (largest) approximation, there were $2(7)$ new entailments in $\mathcal{O}_{\text {UMBC }}, 10(300)$ in $\mathcal{O}_{\text {INR }}$ and $28(176)$ new mappings.
3. Alignment $\mathcal{O}_{\text {AIFB }}, \mathcal{O}_{\text {INR }}$ :for the smallest (largest) approximation, there were 4 (37) new entailments in $\mathcal{O}_{\text {AIFB }}, 2(19)$ in $\mathcal{O}_{\text {INR }}$ and 46 (140) new mappings.

Note that the number of new entailments (and hence the amount of information that ContentMap shows to users) largely depends on the selected approximation.

In all cases we found a significant number of obviously unintended inferences due to inherent disagreements between the ontologies being integrated. For example, when integrating $\mathcal{O}_{\text {AIFB }}$ and $\mathcal{O}_{\text {INR }}$, our tool detected a total of 34 newly unsatisfiable concepts in the two ontologies. The large number of (rather complex) justifications for some of these entailments makes manual repair almost unfeasible. When computing the corresponding plans, we found that the problem was originated by the ranges of two datatype properties, which were incompatible; hence, the modification of two axioms sufficed to fix all the errors at once. In most cases, a significant number of obviously unintended new subsumptions were also detected. For example, merging $\mathcal{O}_{\text {MIT }}$ and $\mathcal{O}_{\text {INR }}$ resulted in the new subsumptions TechnicalReport $\sqsubseteq$ Date and TechnicalReport $\sqsubseteq \exists$ date.Reference. Again, the obtained plans revealed the origin of the problem, see axioms (4-7).

| $\mathcal{O}_{\text {INR }}$ : year | $\sqsubseteq$ | $\mathcal{O}_{\text {MIT }}$ : hasYear |
| ---: | :---: | :--- |
| $\mathcal{O}_{\text {MIT }}$ : TechnicalReport | $\sqsubseteq$ | $\geqslant \mathcal{O}_{\text {MIT }}$ : hasYear 1.Literal |
| $\mathcal{O}_{\text {INR }}$ : TechnicalReport | $\sqsubseteq$ | $\mathcal{O}_{\text {MIT }}$ : Technicalreport |
| $\mathcal{O}_{\text {INR }}$ : year | hasDomain | $\mathcal{O}_{\text {INR }}$ : Date |

Synthetic Repair of Automatically Generated Mappings Having repaired the test ontologies using the gold standard mappings, we used ContentMap to automatically detect and repair errors resulting from the generation of new mappings using the mapping tools OLA ${ }^{6}$, AROMA ${ }^{7}$ and CIDER $^{8}$. Our goal was twofold: first, to show that the algorithms in ContentMap are practical; second, to show that ContentMap can be used to automatically detect and repair errors, as well as to improve the quality of automatically generated mappings.

For each pair of test ontologies, and for various sets of automatically generated mappings, we have performed the synthetic experiments in Table 4, which closely follow our proposed method from Table 3. In contrast to Table 3, however, the repair of errors is performed in two stages: first, the obvious errors (i.e. unsatisfiable concepts); then, those subsumptions that ContentMap heuristically found unintended. For these experiments we have used the smallest approximation of the deductive difference available in ContentMap. The Roman numbers in Table 4 refer to measurements that are stored during the experiment.

Tables with the obtained results are given in Appendix. Here, we summarise the main conclusions drawn from these experiments. First, from a computational point of view, the main bottleneck is the computation of all the justifications for the entailments of interest. Once the justifications have been computed, the time needed for computing the plans is relatively low. Hence, it is important to investigate optimisations for computing all justifications; first steps in this direction have been taken in $[13,14]$.

Second, the number of entailments in the computed differences is similar to the results obtained for the gold standard for the considered approximation, and the number of obtained minimal plans varies from 1-50. Furthermore, the use of the dependencies given in Definition 6 significantly reduces the amount of information that the user would need to examine.

Third, the use of automatically generated mappings did result in the occurrence of a significant number of unintended entailments. For example, when aligning $\mathcal{O}_{\text {AIFB }}$ and $\mathcal{O}_{\text {INR }}$ using CIDER with confidence threshold $\tau=0.1$ (notice that CIDER works mainly with low confidence values), we found 55 new unsatisfiable concepts. After fixing these errors, ContentMap found 34 unintended subsumption relationships using Algorithm 1 for a threshold $\tau_{1}=0.3$. Moreover,

[^3]Table 4. Synthetic Experiments
Input: $\mathcal{O}_{1}, \mathcal{O}_{2}$ : ontologies with $\operatorname{Sig}\left(\mathcal{O}_{1}\right)=\Sigma_{1}, \operatorname{Sig}\left(\mathcal{O}_{2}\right)=\Sigma_{2}$ and $\Sigma_{1} \cap \Sigma_{2}=\emptyset$
$\mathcal{M}$ : automatically-generated mappings between $\Sigma_{1}$ and $\Sigma_{2}, \mathcal{M}_{\mathcal{G}}$ : gold standard
1: Filter $\mathcal{M}$ given a confidence threshold $\tau(\mathbf{I}, \mathbf{I I})$
2: Compute precision (III) and recall (IV) of $\mathcal{M}$ with respect to $\mathcal{M}_{\mathcal{G}}$
3: Compute $\operatorname{diff} \tilde{\widetilde{\Sigma}}_{1}\left(\mathcal{O}_{1}, \mathcal{U}\right)$, $\operatorname{diff} \tilde{\Sigma}_{2}\left(\mathcal{O}_{2}, \mathcal{U}\right)$ and $\operatorname{miff} \tilde{\tilde{\Sigma}}_{1}, \Sigma_{2}(\mathcal{M}, \mathcal{U})(\mathbf{V}, \mathbf{V I})$ for $\mathcal{U}:=$ $\mathcal{O}_{1} \cup \mathcal{O}_{2} \cup \mathcal{M}$
4: Stage 1 (IX)
5: Compute all minimal plans for $\mathcal{U}$ given $\mathcal{O}^{-}=\mathcal{M}, \Im^{+}=\emptyset$, and $\Im^{-}:=$new concept unsatisfiability entailments (XII).
6: Store number of plans (XIII) and extraction time (XIV).
7: Compute $\mathcal{O}_{1}^{\prime}:=\mathcal{O}_{1} \backslash \mathcal{P}, \mathcal{O}_{2}^{\prime}:=\mathcal{O}_{2} \backslash \mathcal{P}, \mathcal{M}^{\prime}:=\mathcal{M} \backslash \mathcal{P}(\mathbf{X V})$, for $\mathcal{P}$ the best plan.
8: Compute precision (XVIII) and recall (XIX) of $\mathcal{M}^{\prime}$ with respect to $\mathcal{M}_{\mathcal{G}}$
Stage 2 (IX)
10: Compute $\Lambda=\operatorname{diff} \widetilde{\Sigma}_{1}\left(\mathcal{O}_{1}^{\prime}, \mathcal{U}^{\prime}\right) \cup \operatorname{diff} \widetilde{\Sigma}_{2}\left(\mathcal{O}_{2}^{\prime}, \mathcal{U}^{\prime}\right) \cup \operatorname{mdiff} \widetilde{\Sigma}_{\Sigma_{1}, \Sigma_{2}}\left(\mathcal{M}^{\prime}, \mathcal{U}^{\prime}\right)(\mathbf{V}, \mathbf{V I})(\mathbf{X V I}$, XVII) for $\mathcal{U}^{\prime}:=\mathcal{O}_{1}^{\prime} \cup \mathcal{O}_{2}^{\prime} \cup \mathcal{M}^{\prime}$

11: Compute dependency relation $\triangleright$ over $\Lambda$
12: Store time of computing $\triangleright($ VIII) and number of roots for $\triangleright$ (VII)
13: Compute all minimal plans for $\mathcal{U}^{\prime}$ given $\mathcal{O}^{-}=\mathcal{M}^{\prime}, \Im^{+}=\emptyset$ and $\Im^{-}(\mathbf{X I}):=$ as obtained in Algorithm 1 for a pre-fixed confidence threshold $\tau_{1}(\mathbf{X})$.
14: Store number of plans (XIII) and extraction time (XIV).
15: Compute $\mathcal{O}_{1}^{\prime \prime}:=\mathcal{O}_{1}^{\prime} \backslash \mathcal{P}, \mathcal{O}_{2}^{\prime \prime}:=\mathcal{O}_{2}^{\prime} \backslash \mathcal{P}, \mathcal{M}^{\prime \prime}:=\mathcal{M}^{\prime} \backslash \mathcal{P}$ (XIV), for $\mathcal{P}$ the best plan.
16: Compute $\Lambda=\operatorname{diff} \widetilde{\Sigma}_{1}\left(\mathcal{O}_{1}^{\prime \prime}, \mathcal{U}^{\prime \prime}\right) \cup \operatorname{diff} \widetilde{\widetilde{\Sigma}}_{2}\left(\mathcal{O}_{2}^{\prime \prime}, \mathcal{U}^{\prime \prime}\right) \cup \operatorname{mdiff} \widetilde{\Sigma}_{1}, \Sigma_{2}\left(\mathcal{M}^{\prime \prime}, \mathcal{U}^{\prime \prime}\right)($ XVI, XVII $)$ for $\mathcal{U}^{\prime \prime}:=\mathcal{O}_{1}^{\prime \prime} \cup \mathcal{O}_{2}^{\prime \prime} \cup \mathcal{M}^{\prime \prime}$
17: Compute precision (XVIII) and recall (XIX) of $\mathcal{M}^{\prime \prime}$ with respect to $\mathcal{M}_{\mathcal{G}}$
we checked manually selected examples and found out that the heuristically detected unintended subsumptions were indeed errors; furthermore, these errors were mostly caused by incorrect mappings.

Fourth, the application of the plans resulted in the automatic correction of the identified errors, which resulted in an improvement in the precision of the automatically generated mappings. The improvement in precision occurred in all cases and varied from $1 \%-5 \%$, achieving a good balance with respect to the recall, which remained unchanged in most cases, although a decrease from $1 \%-3 \%$ was observed in a few isolated cases.

## 5 Related Work and Conclusion

In the last few years, the problem of automatically generating mappings between ontologies has been extensively investigated. An extensive and up-to-date source of information about the topic (including papers, tools, ontologies for evaluation, etc.) can be found at http://www.ontologymatching.org/.

The problem of reasoning with the generated mappings has also received significant attention. Different semantics have been proposed for assigning formal meaning to ontology mappings (e.g. [5, 6]). As mentioned in Section 3, our general approach is applicable regardless of the semantics adopted for the mappings.

Recently, research has been conducted on the debugging and revision of mappings $[1,2]$. This research has so far been focused on mappings represented using Distributed Description Logics (DDL) [6]. Our work is also related to the existing approaches for debugging and repairing inconsistencies in OWL ontologies (e.g. $[15,12,11,13]$ ). In both of these lines of research, the detected and repaired errors are limited to unsatisfiable concepts and inconsistent ontologies.

When compared to this existing work, we believe that our approach presents a number of improvements. First, the entailments to be repaired are not restricted to obvious inconsistencies, but can include any unintended entailment. Second, users can customise the kinds of entailments to be taken into account when comparing the integrated ontology to the individual ones in order to detect errors (i.e. select the approximation of the deductive difference). Third, users can select not only which entailments should be invalidated, but also which ones should necessarily hold upon completion of the repair process. To this end, we provide a number of novel techniques for helping the user to select which entailments are (un)intended, such as the computation of the dependencies between entailments (the relation $\triangleright$ ), confidence in entailments according to the confidence in the mappings, etc. Fourth, we provide efficient algorithms for computing all the repair plans and to help the user select the most suitable plan among those been obtained. Fifth, when compared to existing work on debugging and repair in OWL, we provide a clear distinction between the ontologies being integrated and the mappings, and users can customise the ontologies from which the plans are allowed to delete axioms. Finally, we provide a fully-fledged editor and reasoning infrastructure integrated with Protégé 4.

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## Appendix: Result Tables

|  |  | $\left\lvert\, \begin{gathered} \infty \\ \infty \\ 0 \\ \hline \end{gathered}\right.$ | $\begin{gathered} \infty \\ \infty \\ 0 \\ 0 \end{gathered}$ | $\infty_{\infty}^{\infty}$ | $\infty_{\infty}^{\infty} \underset{\infty}{\infty}$ | $\begin{array}{\|c\|c} \infty & 1 \\ \infty \\ \hline & \infty \\ \hline \end{array}$ |  | $\begin{gathered} \bar{\infty} \\ 0 \\ 0 \end{gathered}$ | $\left\lvert\, \begin{array}{cc} 1 \\ & 1 \\ 0 \end{array}\right.$ |  | $\stackrel{1}{0}$ | N |  | ，N |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \bar{a} \\ & 00 \\ & 0 \\ & 5 \end{aligned}$ |  |  | $\left\lvert\, \begin{array}{l\|l\|} \hline 0 \\ 0 \\ 0 \end{array}\right.$ | $\left\lvert\, \begin{array}{ll} 1 \\ 0 & 2 \\ 0 \\ 0 \end{array}\right.$ | $\stackrel{R}{i} .$ | $\begin{array}{l\|l\|l\|l\|l\|l\|l\|l\|l\|l\|l\|l\|l\|l\|l\|l\|l\|l\|l\|l\|l\|} \hline \end{array}$ | $\begin{aligned} & 8 \\ & \hline .8 \\ & \hline .0 \\ & \hline 0 \\ & 0 \end{aligned}$ | $\underbrace{0}_{0}$ | $\left\lvert\, \begin{array}{cc} \wedge \\ \\ 0 \\ 0 & \infty \\ 0 \end{array}\right.$ |  | $\left\|\begin{array}{l} - \\ \infty \\ 0 \end{array}\right\|$ | $\begin{aligned} & \infty \\ & \infty \\ & 0 \\ & 0 \\ & 0 \end{aligned} 0_{0}$ |  | ， $\begin{gathered}\infty \\ 0 \\ 0\end{gathered}$ |
| $\frac{\sim}{4}$ |  | $\bigcirc$ | \％ | $\infty$ | 악 | $\therefore 10$ | 악 | 18 | $\bigcirc \mathrm{O}$ |  | 1 ¢ | Nos |  | 1 N |
| $\left\lvert\, \begin{aligned} & \stackrel{y}{4} \\ & 4 \end{aligned}\right.$ | $\begin{array}{\|c\|c} 2 \\ x & 2 \\ x & 0 \\ 0 \end{array}$ | む | ～ | ～ |  |  | $\cdots$ | $\sim$ | $\lessdot \sim$ | I | ＝ | 20 | 2 | $\because$ |
|  | $\begin{array}{\|l\|l\|} \hline x & z \\ \hline \end{array}$ | $\mathscr{2}$ | $\underset{A}{2}$ | $\begin{array}{l\|l} 20 & 0 \\ -1 & \\ \hline \end{array}$ | $0$ | ৪\| | O゙， | ® | 込发 |  | 8 | $\stackrel{2}{2}$ | ＋ | － |
|  |  | $\left\lvert\, \begin{gathered} 0 \\ \mathbb{N} \end{gathered}\right.$ | $\begin{aligned} & \hline \\ & 0 \\ & 0 \\ & \hline \end{aligned}$ | $\begin{array}{\|l\|l} \hline 0 & 0 \\ \infty & 0 \\ 0 & 0 \\ 0 \end{array}$ |  | $\begin{array}{\|ll} \hline- \\ \stackrel{\rightharpoonup}{n} & 0 \\ \hline \end{array}$ |  | $0$ | $\left\lvert\, \begin{array}{ll} n \\ 0 & 0 \\ 0 \end{array}\right.$ |  | $\begin{array}{l\|l\|} \hline \\ \hline \\ 0 \\ \hline \end{array}$ | （ | $\bigcirc$ | 1 ${ }^{\circ}$ |
|  | 有 | 7 | $\bigcirc$ | \％ 0 | － | 010 | $\bigcirc$ | $\infty$ | $\underset{\sim}{\infty} \sim$ | N | $\sim$ | $\cdots$ | $=0$ | － |
|  | $\begin{array}{\|l\|l} \mathrm{A} & -1 \\ \mathrm{x} & -1 \end{array}$ | 20 | $\bigcirc$ | $\bigcirc$ |  | 20 | 9 | $\bigcirc$ | 20 | 0 | $\bigcirc$ | $0 \cdot$ |  | 0 |
|  |  |  | － |  | $\pm$ | $\infty$ | －＇ | － | 1 ～ | ，＇ | $\sim$ | ＇ | ， | $\sim$ |
| $\mid$ | $\begin{array}{\|l\|l\|} \hline x & \vec{y} \\ \hline \end{array}$ |  | $\bigcirc$ | OR | $\bigcirc$ | ．${ }^{1} \stackrel{10}{0}$ | － | ＋ | －$\stackrel{20}{2}$ | － | $1 \begin{gathered} 12 \\ \hline 0 \\ \hline 0 \end{gathered}$ | 1 | － | $1 \overrightarrow{0}$ |
|  |  | $-1$ |  |  |  | －1 ${ }^{\circ}$ | $\rightarrow$ | 次 | 匀 | $\bigcirc$ | 仡 | － 20 |  | 18 |
|  |  |  | $\begin{gathered} \infty \\ 1 \\ -1 \end{gathered}$ | 20 | 200 |  | － | $\xrightarrow[\sim]{\text { N }}$ | ， | － | $\stackrel{1}{0}$ | ． 2 |  | ， $\begin{array}{r}\bullet \\ \hline 1.0 \\ -1 \\ \hline\end{array}$ |
|  | $\begin{array}{\|l\|l} \hline 7 & \Delta \\ \hline 8 & \triangle \end{array}$ |  | $\bigcirc$ | Lin | $\stackrel{\circ}{\circ}$ | ＇ 28 | \％ | $\stackrel{18}{7}$ | ¢ | 8 | 8 | ＇ |  | 2 |
| $n$ | B | $\bigcirc$ | $\infty$ | $\ldots$ | $\infty$ | \％ | － | 1 | 120 | 0 | 8 | \％ | $\stackrel{3}{5}$ | $\cdots$ |
|  |  | 20 | ジ | $\bigcirc$ | $\cdots$ | $\stackrel{1}{\sim}$ | － | $\infty$ | $\because$ | $\bigcirc$ | $\%$ | $\stackrel{\sim}{\circ}$ | 2 | 2 |
| $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $$ | $\left\lvert\, \begin{aligned} & \infty \\ & \infty \\ & \hline-\infty \end{aligned}\right.$ | $\left(\begin{array}{l} \infty \\ 0 \\ 0 \end{array}\right.$ |  | $\infty_{\infty}^{\infty}$ | $\begin{array}{c\|c} \infty & \infty \\ \infty & \infty \\ 0 \\ \hline \end{array}$ |  | $\underbrace{\infty}_{0}$ |  | $\dot{\dot{c}} \underset{0}{\circ}$ | $\left\lvert\, \begin{aligned} & \stackrel{0}{0} \mid \end{aligned}\right.$ | $\begin{aligned} & \mathrm{N} \\ & \mathrm{~N} \\ & 0 \\ & 0 \end{aligned}$ |  | $$ |
|  | $$ | $0$ |  |  | $\hat{C}_{0}^{2}$ | $\begin{array}{\|c\|c} \infty \\ \infty \\ 0_{0} & \infty \\ 0 \\ \hline \end{array}$ |  |  | $\begin{array}{\|c\|c}  & N \\ N & N \\ 0 & 0 \\ \hline \end{array}$ | $\dot{0} \underbrace{\infty}_{0}$ |  | $\begin{array}{\|c\|c\|c\|c\|c\|c\|} \infty & \alpha \\ 0 & \alpha \\ 0 & \alpha \\ \hline \end{array}$ |  | （1） |
|  | $\square$ | $\ddot{9}$ | $\underset{\sim}{2}$ | $\frac{\infty}{2}$ | $\stackrel{20}{7}$ | $\bigcirc$ | 8 | O゙ | － 10 | $\bigcirc$ | R | O20 |  | O |
|  |  |  |  | No |  | $\begin{aligned} & 1 \\ & 0 \\ & \hline \end{aligned}$ |  | $\underset{0}{\circ}$ | No |  | $\mathfrak{O}$ | $\stackrel{-}{0}$ |  | No |
| $\left\|\begin{array}{l} \underset{\sim}{~} \\ \underset{己}{~} \end{array}\right\|$ |  |  |  |  | $\stackrel{\square}{1}$ |  |  |  |  | $\stackrel{\sim}{\sim}$ |  |  | 10 |  |
| $\left\|\begin{array}{l} \mathbb{N} \\ \sim \end{array}\right\|$ |  |  |  |  | $\bigcirc$ |  |  |  |  | ～ |  |  | $\stackrel{\square}{\square}$ |  |
| $\begin{array}{\|c\|} \hline 0 \\ 0 \\ \hline \end{array}$ | $\sum^{0}$ |  |  |  | $\propto$ |  |  |  |  | ¢ |  |  | $\stackrel{3}{7}$ |  |
|  | $\begin{aligned} & 0 \\ & 2 \\ & 0 \\ & 0 \end{aligned}$ |  |  |  | $\begin{aligned} & \frac{\infty}{2} \\ & 0_{0}^{6} \\ & 2 \\ & 2 \\ & 0 \\ & 0 \end{aligned}$ |  |  |  |  | $\begin{aligned} & \stackrel{\breve{w}}{\sum_{0}^{2}} \\ & 0 \\ & 2 \\ & 2 \\ & 0 \\ & 0 \end{aligned}$ |  |  | $\begin{aligned} & \sum_{0}^{n} \\ & 2 \\ & 2 \\ & 0 \end{aligned}$ |  |

Table 5．Results with CIDER


Table 6. Results with AROMA

| $\mathcal{O}_{1} \sim \mathcal{O}_{2}$ | Gold Standard |  |  | Tool Results |  |  |  |  |  |  |  | Repair Information |  |  |  |  |  | After Applying Plan |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathcal{M}_{\mathcal{G}}$ | $\text { diff } \approx$ | mdiff $\approx$ | I | II | III | IV | V | VI | VII | VIII | IX | X | XI | XII | XIII | XIV | XV | XVI | XVII | XVIII | XIX |
|  |  |  |  | $\tau$ | $\mathcal{M}$ | Precision | Recall | diff $\approx$ | mdiff $\approx$ | $\triangleright$ | $\mathcal{J}$ ( s ) | Stage | $\tau_{\text {del }}$ | $\Im^{-}$ | $\perp$ | P | $\mathbb{P}_{\text {t }}(\mathrm{s})$ | $\mathcal{M}$ | diff $\approx$ | mdiff $\approx$ | Precision. | Recall |
| $\mathcal{O}_{\text {INR }} \sim \mathcal{O}_{\text {AIFB }}$ | 98 | 6 | 46 | 0.7 | 90 | 0.86 | 0.79 | 44 | 5 | - | - | $\perp$ | - | - | 44 | 4 | 496.5 | 89 | 16 | 57 | 0.87 | 0.79 |
|  |  |  |  |  | 89 | 0.87 | 0.79 | 16 | 57 | 52 | 41.1 | $\Im^{-}$ | 0.5 | 1 | 0 | 4 | 0.00 | 88 | 4 | 44 | 0.88 | 0.79 |
| $\mathcal{O}_{\text {INR }} \sim \mathcal{O}_{\text {UMBC }}$ | 83 | 12 | 28 | 0.7 | 88 | 0.58 | 0.61 | 22 | 38 | - | - | $\perp$ | - | - | 12 | 86 | 363.8 | 87 | 14 | 51 | 0.58 | 0.6 |
|  |  |  |  |  | 87 | 0.58 | 0.6 | 14 | 51 | 60 | 869.5 | $\bigcirc$ | 0.55 | 16 | 0 | 30 | 0.42 | 80 | 2 | 26 | 0.63 | 0.60 |
| $\mathcal{O}_{\text {INR }} \sim \mathcal{O}_{\text {MIT }}$ | 119 | 16 | 35 | $0.7$ | 60 | 0.83 | 0.42 | 26 | 46 | - | - | $\perp$ | - | - | 0 | 0 | - | - | - | - | - | - |
|  |  |  |  |  | 60 | 0.83 | 0.42 | 26 | 46 | 29 | 26.4 | $\Im^{-}$ | 0.55 | 20 | 0 | 8 | 0.04 | 59 | 2 | 16 | 0.85 | 0.42 |

Table 7. Results with OLA


[^0]:    ${ }^{3}$ The development of an ontology describing types of juvenile arthritis is one of the goals of the Health-e-Child project (http://www.health-e-child.org/).

[^1]:    ${ }^{4}$ A logiC-based ONtology inTEgratioN Tool using MAPpings

[^2]:    ${ }^{5}$ http://oaei.ontologymatching.org/2004/Contest/

[^3]:    ${ }^{6}$ OWL Lite Alignment: http://ola.gforge.inria.fr/
    ${ }^{7}$ AROMA: http://www.inrialpes.fr/exmo/people/jdavid/
    ${ }^{8}$ CIDER: http://sid.cps.unizar.es/SEMANTICWEB/ALIGNMENT/

